

# Analysis of Sub synchronous Resonance Using Simulation of IEEE FIRST BENCHMARK Model

<sup>1</sup>Avani H. Ranpariya, <sup>2</sup>Parth N. Dave

<sup>1</sup>P.G. Student (Electrical Power System), <sup>2</sup>P.G. Student (Electrical Power System)  
Electrical Engineering Department,  
V. V. P. Engineering College, Rajkot, India.  
<sup>1</sup>[avaniranpariya@rediffmail.com](mailto:avaniranpariya@rediffmail.com), <sup>2</sup>[dave.parth009@gmail.com](mailto:dave.parth009@gmail.com)

**Abstract** - The benchmark model for the study sub synchronous resonance is presented by IEEE committee. Here IEEE First benchmark system for Sub synchronous Resonance Analysis is simulated using MATLAB. The Oscillations because of Sub Synchronous Resonance are observed between turbine generator and various turbine shafts. For reducing oscillations or to mitigate Sub synchronous resonance phenomena FACTS device (Flexible AC transmission system) is used. This paper represents analysis of sub synchronous resonance using MATLAB Simulation.

**Index Terms** – SSR, series compensation, transient torque, synchronous machine, torsional oscillation

## I. INTRODUCTION

Series capacitor compensation in AC transmission systems is an economical means to increase load carrying capability, control load sharing among parallel lines and enhance transient stability. However, capacitors in series with transmission lines may cause sub synchronous resonance that can lead to turbine-generator shaft failure and electrical instability at oscillation frequencies lower than the normal system frequency. Therefore, the effects of SSR must be fully understood and analyzed when planning series capacitor compensation in power systems. The main concern with SSR is the possibility of shaft damage from torsional stresses. Damage can result from the long term cumulative effects of low amplitude torsional oscillations or the short term effects of high amplitude torques. Typically, hydro units have mechanical parameters that are less prone to SSR problems than thermal units [3].

Sub synchronous oscillations were first discussed in 1937 and until 1971, shaft torsional oscillations were neglected. Two shaft failures at the Mohave Generating Station in Southern Nevada led to the understanding and development of the theory of interaction between series capacitor compensated lines and the torsional modes of steam turbine-generators [1]. After the second shaft failure at Mohave, the utility industry devoted considerable effort to the analysis and suppression of the SSR phenomenon.

## II. TYPES OF SSR INTERACTION

There are three types of SSR interactions which are Induction Generator Effect, Torsional Interaction Effect and Transient Torque Effect.

### A. Induction Generator Effect

Three phase current at sub synchronous frequency can result due to a nearby network disturbance. When the sub synchronous frequency currents flow through the generator armature, they view the synchronously rotating rotor's circuit as negative resistance. If this negative resistance is greater than the sum of the armature and network resistance, the electrical system is self-excited. Such self-excitation would be expected to result in excessive voltage and current [2]

### B. Torsional Interaction

Torsional interaction occurs when the induced sub synchronous torque in the generator is close to one of the torsional natural modes of the turbine generator shaft. When this happens, generator rotor oscillations will build up and this motion will induce armature voltage components at both sub synchronous and super synchronous frequencies. Moreover, the induced sub synchronous frequency voltage is phased to sustain the sub synchronous torque. If this torque equals or exceeds the inherent mechanical damping of the rotating system, the system will become self-excited. This phenomenon is called "torsional interaction."

### C. Transient Torque

Transient torques is those that result from system disturbances. System disturbances cause sudden changes in the network, resulting in sudden changes in currents that will tend to oscillate at the natural frequencies of the network. In a transmission system without series capacitors, these transients are always dc transients, which decay to zero with a time constant that depends on the ratio of inductance to resistance. For networks that contain series capacitors, the transient currents will be of a form similar to above equation, and will contain one or more oscillatory frequencies that depend on the network capacitance as well as the inductance and resistance. In a simple radial R-L C system, there will be only one such natural frequency, which is exactly the situation described in above equation, but in a network with many series capacitors there will be many such Sub synchronous frequencies. If any of these sub synchronous network frequencies coincide with one of the natural modes of a turbine-generator shaft, there can be peak torques that are quite large since these torques are directly proportional to the magnitude of the oscillating

current. Currents due to short circuits, therefore, can produce very large shaft torques both when the fault is applied and also when it is cleared. In a real power system there may be many different sub synchronous frequencies involved and the analysis is quite complex.

**III. IEEE FIRST BENCHMARK MODEL**

The single line diagram of a Single Machine Infinite Bus system given by IEEE committee for SSR study is shown in fig 1

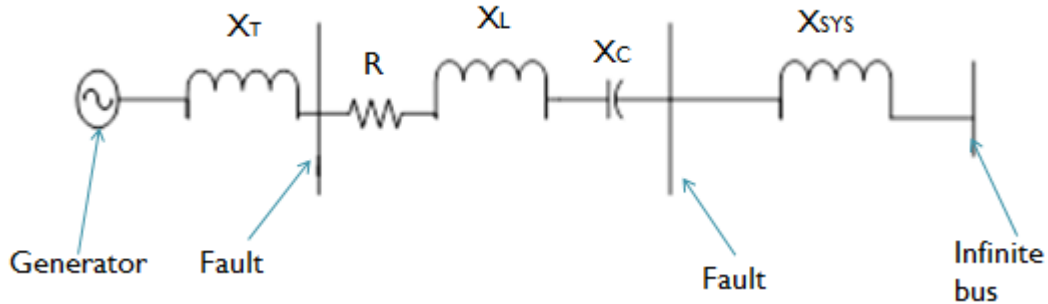


Fig. 1: Single line Diagram for IEEE first benchmark system

The circuit parameters are expressed in per unit on the generator MVA rating at 60Hz. Reactance are proportional to frequency, resistances are constant. The infinite bus is a 3-phase 60 Hz voltage source with zero impedance at all frequencies.

**A. Synchronous Machine Model**

Simple model of synchronous generators are not suitable for accurate description of the power results in time invariant machine equations. So we consider machine in the park reference frame which is rotor reference frame with one damper winding in D-axis and two damper winding in Q-axis shown in fig 2

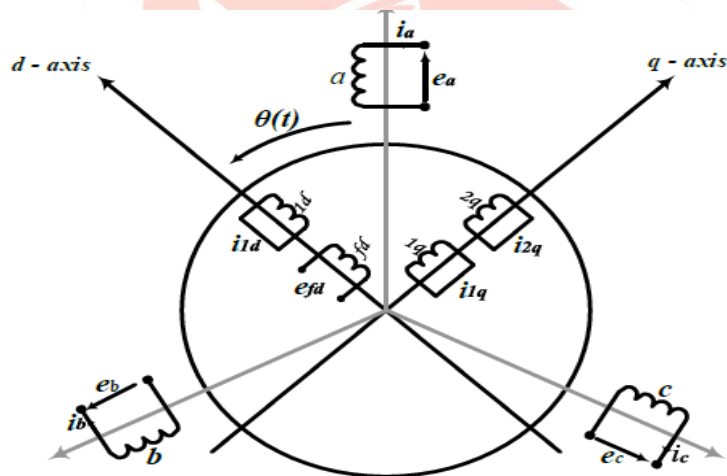


Fig. 3: Schematic diagram of conventional synchronous machine

This model shows three phase armature winding on stator i.e. a, b and c and four winding on the rotor including field winding 'f'. The damper winding is represented by equivalent damper circuit in the direct axis and quadrature axis: 1d on d-axis and 1q and 2q on q-axis.

Two equivalent rotor circuits are represented in each axis of the rotor - F and D in the d-axis, and G and Q in the q-axis, with positive current direction defined as the direction causing positive magnetization of the defined d- and q-axis direction[4], respectively. Synchronous machine operation under balanced three-phase conditions is of particular interest for SSR analysis.

In first IEEE benchmark system circuit parameters are expressed in per unit on the generator base of 892.4 MVA, 60 Hz frequency. Reactance is proportional to frequency and resistances are constant. This system configuration corresponds to the Navajo Project's 892.4 MVA, 500 kV transmission systems.

**B. Multi Mass Model of the Turbine- Generator shaft**

The turbine-generator mechanical system consists of six masses; high-pressure turbine (HP), intermediate-pressure turbine (IP), low pressure turbine A (LPA) and low pressure turbine B (LPB), an exciter (EXC), and a generator (GEN) coupled to a common shaft as shown in Fig.2. The turbine masses, generator rotor and exciter are considered as lumped masses (rigid body) connected to each other via massless springs [4].



Fig. 4: Mechanical structure of six mass FBM systems

From fig 3 the torques acting on the generator mass is:

Generator:

$$\begin{aligned} \text{Input torque } T_{GENin} &= K_{GB} (\Delta\delta_B - \Delta\delta) & (1) \\ \text{Output torque } T_{GENout} &= \Delta T_e - K_{EG} (\Delta\delta - \Delta\delta_E) & (2) \\ \text{Damping } T_{GENdamping} &= D_G \Delta\omega & (3) \end{aligned}$$

Low pressure turbine B:

$$\begin{aligned} \text{Input torque } T_{LPBin} &= \Delta T_{LPB} + K_{BA} (\Delta\delta_A - \Delta\delta_B) & (4) \\ \text{Output torque } T_{LPBout} &= K_{GB} (\Delta\delta_B - \Delta\delta) & (5) \\ \text{Damping } T_{LPBdamping} &= D_B \Delta\omega_g & (6) \end{aligned}$$

Similarly all other masses torque equation can be derived.

**IV. SIMULATION AND RESULTS**

MATLAB simulation for IEEE first benchmark system is shown in fig 4

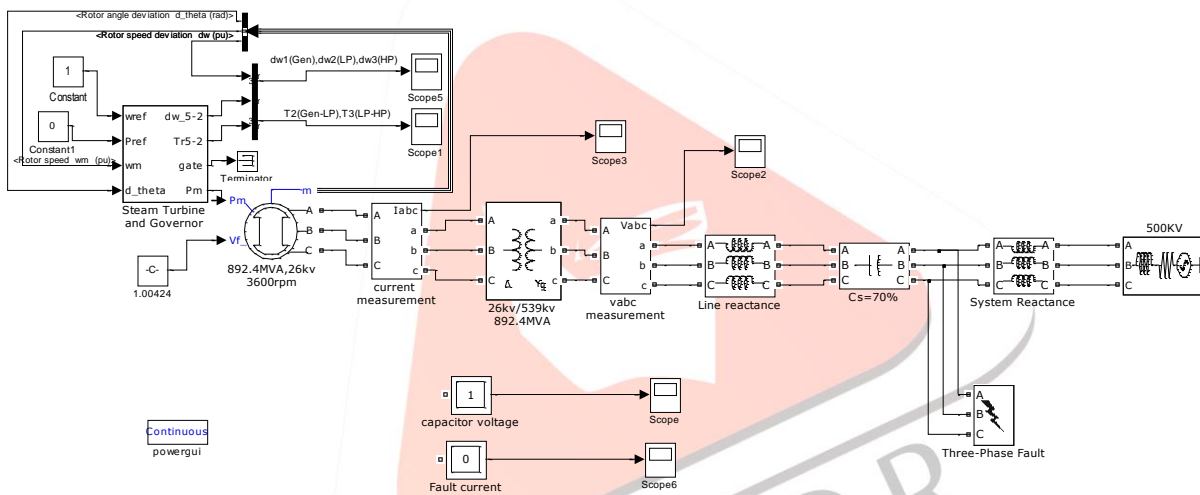


Fig. 4: MATLAB simulation for IEEE First Benchmark system

The machine and circuit parameters are real value taken from the Navajo Project [Appendix]. For the transient case, single phase to ground fault is applied as shown in figure 4 for duration of 80 msec(4 cycle) from 0.1 seconds to 0.175 seconds. In the reference paper, fault reactance is 0.04 p.u. and it is adjusted to produce a capacitor transient voltage approaching the lower gap setting.

Capacitor voltage, Generator current, Generator Electrical Torque, Shaft Torque, speed is plotted for the time duration 1.0Second.

Fig.5 shows variation of Electrical torque of the synchronous generator. It is clear that the torque is not constant for some times after application of fault. That shows the electrical transmission network resonant frequency matches one of the natural modes of the multimass turbine. Fig. 6 shows the shaft torque. From the graph, it is seen that the shaft torque oscillates due to SSR phenomena. Fig. 8 shows the variation of voltage across the capacitor due to SSR.

Fig. 9 shows the variation of the machine current in per unit. From the graph, it is seen that the machine phase current is oscillatory.

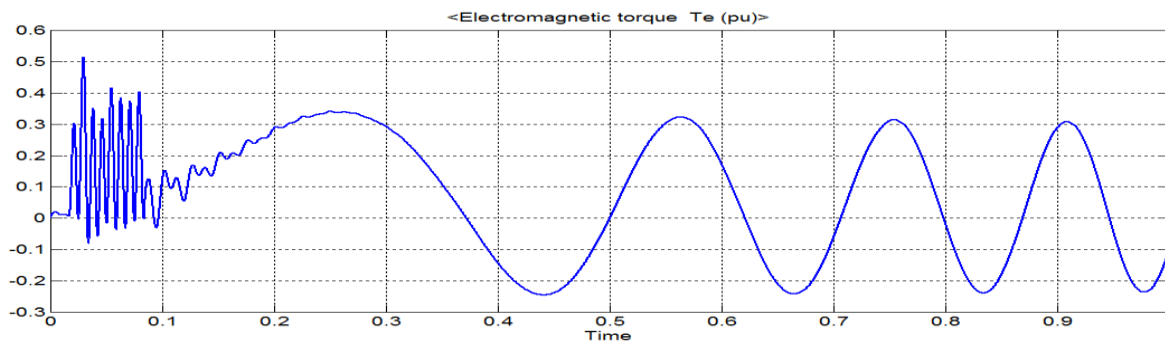


Fig. 7: Variation of electromagnetic torque

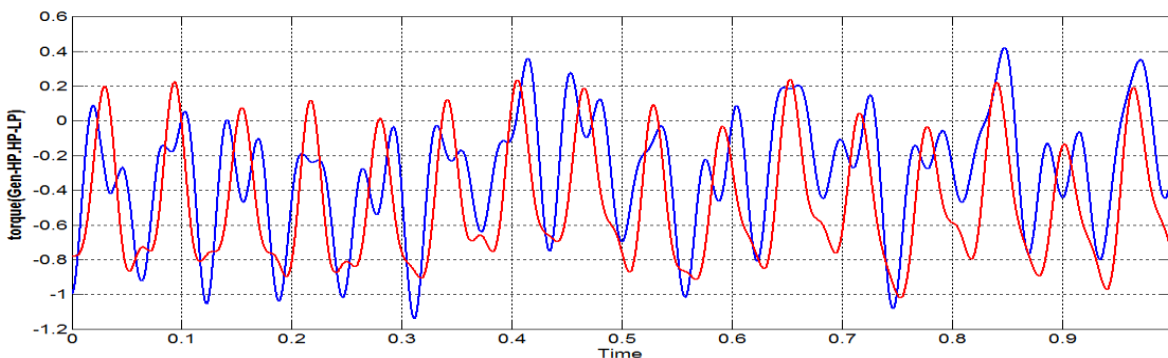


Fig. 8: Variation of shaft torque

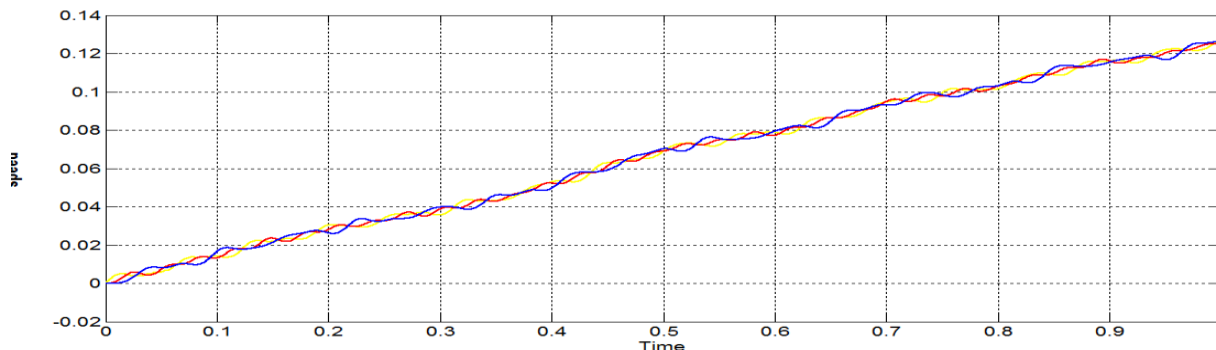


Fig. 9: Waveform for shaft speed(pu)

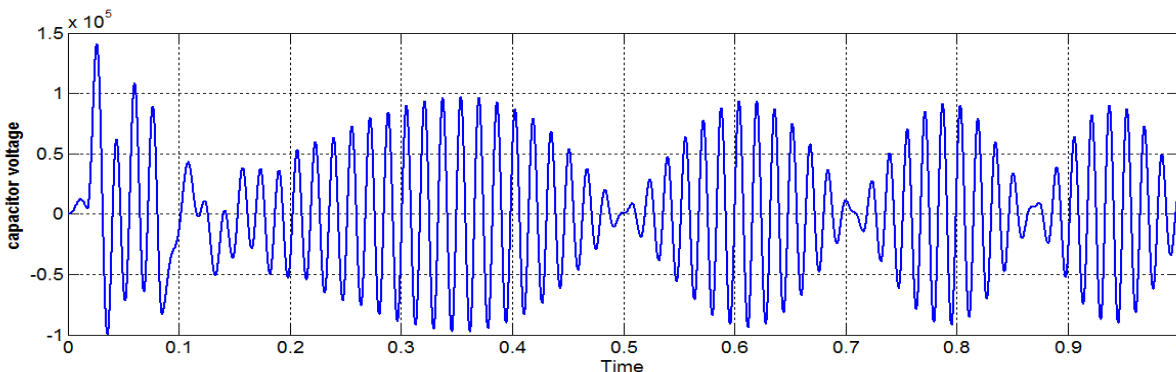


Fig. 10: Variation in capacitor voltage

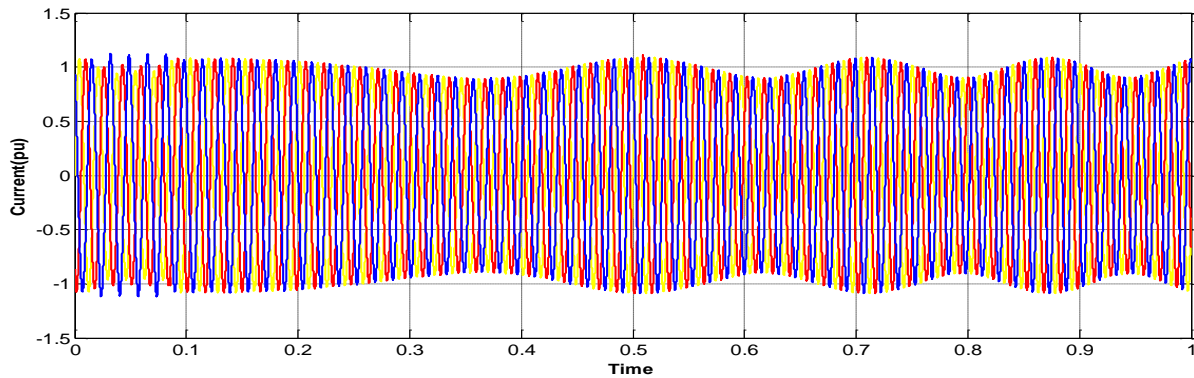


Fig. 10: Variation in system current

**V. CONCLUSION**

Sub synchronous resonance effect is studied using IEEE First Benchmark system and the results have been investigated. It is observed that series compensation produces Sub synchronous resonance, during fault conditions. Sub synchronous Resonance Phenomena is simulated by exciting the torsional modes with single phase to ground fault for duration of four cycles. Result shows that Electromagnetic torque and voltage across the capacitor are highly distorted

**Appendix**

Network parameter of the system is as follows:

**A. Generator parameters**

- Rated MVA: 892.4
- Rated voltage: 26.0kv
- Power factor: 0.9 lagging

Table-1:Parameters of generator

| Parameter | Value   | Parameter  | Value   |
|-----------|---------|------------|---------|
| $X_a$     | 0.13pu  | $X_d$      | 1.79pu  |
| $X_d'$    | 0.169pu | $X_1$      | 0.135pu |
| $X_q$     | 1.71pu  | $X_q'$     | 0.228pu |
| $X_q''$   | 0.2pu   | $R_a$      | 0.002pu |
| $T_{d0}'$ | 4.3s    | $T_{d0}''$ | 0.032s  |
| $T_{q0}'$ | 0.85s   | $T_{q0}''$ | 0.05s   |

Table-2: Mechanical Parameters

| Mass | Inertia (second) | Torque fraction | Shaft     | Spring Constant |
|------|------------------|-----------------|-----------|-----------------|
| HP   | 0.0929           | 0.30            | HP - IP   | 7277pu          |
| IP   | 0.1556           | 0.26            | IP – LPA  | 13168pu         |
| LPA  | 0.8587           | 0.22            | LPA – LPB | 19618pu         |
| LPB  | 0.8842           | 0.22            | LPB - GEN | 26713pu         |
| GEN  | 0.8686           |                 |           |                 |

➤ **Transformer parameter**

- Rated MVA : 892.4
- Voltage rating : 26/539kv
- Delta/star grounded
- $R = 0.00792$  pu
- $X = 0.14$  pu,
- $X_0 = 0.14$  pu

➤ **Transmission line parameter**

- $R = 0.02$ pu,
- $X = 0.50$ pu

➤ **Series capacitor**

$$C = 0.371\text{pu}$$

➤ **Infinite bus**

Voltage: 500kv,

Phase angle:  $0^\circ$

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